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### AXISYMMETRIC DAMPING OF CYLINDRICAL CAVITY MODES BY SHEET DAMPERS



Mission Research Corporation 735 State Street Santa Barbara, California 93101

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# SECTION 1 INTRODUCTION

One of the most undesirable concomitants of simulating SGEMP in a vacuum tank is that cavity oscillations are excited. Because the Q (Q is defined as the number of periods necessary for the energy to decay to e<sup>-1</sup> times its initial value) of these tanks is much larger than 1, the cavity oscillations can interfere with the experiment for the entire duration of the data taking, after a time interval equal to the clear time of the tank. To rid the experiment of these oscillations a number of dampers have been suggested. In analyzing the effect of these dampers different methods have been used. This report will concern itself with, hopefully, elucidating the effect of one of these types of dampers using a modal-type analysis.

A damper which is inexpensive and easy to construct (relative to other types of dampers) is the membrane damper. M. Messier¹ has evaluated the effect of a one and two sheet, membrane damper using a reflection coefficient analysis. Although this type of analysis does not directly utilize the concept of energy absorption in the membrane the reflection coefficient analysis has been shown, by M. A. Messier,² to be nearly equivalent to an analysis which does use the concept of energy absorption. Nevertheless, it is important to describe "how" the membrane damper actually damps modal oscillations. In this report we first investigate how the damper works by some heuristic arguments and then a more exact analysis is done. These heuristic arguments will be made in Section 2. The more exact analysis is made for a one or two sheet damper, and can be used to evaluate

the transverse magnetic mode damping for a cylindrical tank. This latter analysis is contained in Section 3 and is based upon modal arguments similar to those of W. A. Seidler<sup>3</sup> and C. Baum.<sup>4</sup> In Section 3, our derivation of the more exact equations for a damper analysis will assume that the damper sheets are cylinders with no end caps. (The heuristic analysis suggests that end caps might decrease the Q of the tank by a factor proportional to the area of the end caps, for modes which have an electric field in the radial direction.)

Part of the conclusions which can be drawn from the heuristic analysis of Section 2 are based upon assuming that the modes of the tank are not appreciably changed by the damper sheets. Although the relations derived in Section 2 show how the variation of parameters effect damping, they can't really be used to design a damper; the relations are too inaccurate. In Section 3.2 we make a first order approximation, to the exact equations derived in Section 3.1, to obtain an accurate approximation of the relationship between modes, damper positions and sheet resistance. The first order approximation is based on assuming that the modes do not appreciably change when damper sheets are introduced in the tank.

In Section 4 the results of Sections 2 and 3 are compared and further conclusions are drawn. Graphs and tables are presented that should be useful in designing sheet dampers. Finally in Section 5 we summarize our results and conclusions.

# SECTION 2 HEURISTIC ANALYSIS OF MEMBRANE DAMPER

We shall try to show, in a somewhat heuristic way, what physics goes into a sheet damper analysis; the sheet damper is contrasted with damping due to cavity walls of finite conductivity. In our analysis, we will demonstrate what parameters the Q of the cavity depends upon. We will also get a ball park numerical answer for sheet resistance. We explicitly consider only one damper sheet. If  $\mathscr E$  is the energy in a cavity then the rate of change of the energy is the Joule heat loss:

$$\frac{\mathrm{d}\mathscr{E}}{\mathrm{dt}} = -\int \vec{J} \cdot \vec{E} \mathrm{dV} , \qquad (1)$$

where  $\vec{J}$  is the current in the sheet and  $\vec{E}$  is the electric field in the sheet. If A is the area of the sheet, d its thickness,  $\sigma$  its conductivity and E, the field parallel to the sheet then

$$\frac{\mathrm{d}\mathscr{E}}{\mathrm{d}t} = -\mathrm{Ad}\sigma E_{ii}^2 , \qquad (2)$$

where we have assumed that the current in the sheet is related to  $\vec{E}$  by

$$\vec{J} = \sigma \vec{E} ,$$

and that  $\vec{E}$  is roughly constant over the thickness d. This latter condition is satisfied if

$$\frac{\delta}{d} = \frac{c}{2\pi} \sqrt{\frac{\tau R_e}{d}} >> 1 , \qquad (3)$$

where  $\delta$  is the skin depth for a mode which has the period  $\tau$  and a sheet whose resistance is  $R_{\underline{e}}(\sec/cm)$  .

To relate the parameters in Equation 2 to the Q of the cavity we must relate  $E_{ii}^2$  to the energy in the cavity. In general

$$\mathscr{E} = 2VE^2 , \qquad (4)$$

where V is the volume of the cavity. Also, we may have

$$E_{ij}^2 \simeq E^2 . ag{5}$$

Combining Equations 4, 5 and 2 we find

$$\frac{\mathrm{d}\mathscr{E}}{\mathrm{d}t} = -\frac{1}{2} \left( \frac{\mathrm{Ad}}{\mathrm{V}} \right) \, \, \sigma\mathscr{E} \quad . \tag{6}$$

Defining the Q of the cavity as the number of periods,  $\tau$ , for the energy to decay to  $e^{-1}$  of its initial value, we find that

$$Q = \left(\frac{2}{\sigma\tau}\right)\left(\frac{V}{Ad}\right) , \qquad (7)$$

where

$$\frac{\mathrm{d}\mathscr{E}}{\mathrm{d}t} = -\frac{1}{0\tau}\mathscr{E},\tag{8}$$

if the damper does not charge the period appreciably. For a cylindrical cavity, of radius R the period  $\tau$  of the 1st mode can be approximated by

$$\tau \simeq \frac{2.4R}{c} . \tag{9}$$

Substituting (9) into (7) we find that the Q for the 1st mode is approximated by

$$Q \simeq \frac{1}{2.4} \left( \frac{R}{R_0} \right) cR_e , \qquad (10)$$

where we have made use of the relations

$$V = \pi R^2 h , \qquad (11)$$

$$A = 2\pi R_0 h , \qquad (12)$$

$$R_{\rho} = (\sigma d)^{-1} . \tag{13}$$

In Equation 12 we have assumed that the area of the damper comes from a cylindrical sheet of radius  $\mathbf{R}_0$  with no end caps. Equation 10 is the equation we are seeking.

We can obtain a ball park estimate of the sheet resistance  $\mathbf{R}_{\underline{e}}$  from Equation 10:

$$R_{e} = 2.4 \frac{Q}{c} \left(\frac{R_{0}}{R}\right) \frac{\sec}{cm}$$

$$= 72 Q \left(\frac{R_{0}}{R}\right) (ohm) , \qquad (14)$$

if  $R_0/R$  = .8 and Q = 1 then  $R_e$  is 58 ohms. That is we should expect a sheet resistance of the order of 100 ohms. Q equal to 1 is about the smallest value Q can have without appreciably changing the period of the mode;  $R_0/R$  equal to 18 is a convenient position for the damper.

Equation 10 suggests that the Q can be made smaller by reducing the resistance  $\rm R_e$  or increasing the sheet position radius  $\rm R_0$ . The actual relationship between  $\rm R_0$ ,  $\rm R_e$  and Q for a given mode, however, depends upon how the fields actually vary with position in the cavity and is more complex than Equation 10. (For example, in the present discussion we assumed that the electric field parallel to the damper is constant in the cavity, whereas, in fact, it vanishes at the walls of the cavity.) With an accurate calculation Q is minimized with respect to  $\rm R_0$  and  $\rm R_e$ .

We can get an impression of how end caps on the conducting sheet might affect the damping by investigating Equation 7. From Equation 7 we see that the Q of a cavity is inversely proportional to the area. The ratio of the area of a cylinder with end caps to one with no end caps is (1 + R/h). For h equal to 6 meters and R equal to 2 meters this ratio would be 4/3. A damper which was a complete cylinder might have a Q about 25 percent smaller

than a damper which has no end caps. This latter statement has meaning only for modes which have electric fields in the radial direction; in general the energy in the radial electric field should be about equal to the energy associated with the electric field in the z direction.

From Equation 10, we can understand how sheet damping differs from that of damping due to the walls of the tank alone. If  $R_0$  = .8R, in Equation 10, then

$$Q \cong .33 \text{ cR}_{e} . \tag{15}$$

From Reference 5 the Q for the lowest mode of a cavity,  $\overline{\mathbb{Q}}$ , whose length is three times its radius is

$$\overline{Q} = \frac{3}{8\pi} \frac{R}{\delta} \quad . \tag{16}$$

Equation 16 expresses the Q for a cavity whose damping depends only on the finite conductivity of its walls. A bar over a quantity will refer to this latter cavity.  $\overline{\delta}$  is the skin depth and is given by

$$\overline{\delta} = \frac{c}{2\pi} \sqrt{\frac{\tau}{\sigma}} \quad . \tag{17}$$

Using Equation 9 to approximate  $\overline{\delta}$  we have

$$\overline{\delta} \sim \frac{1}{4} \sqrt{\frac{Rc}{\overline{\delta}}} \quad . \tag{18}$$

Substituting (18) into (16) we find that

$$\overline{Q} \simeq (.48) \frac{\overline{\sigma}R}{c}$$
 (19)

If we define an effective "sheet resistance" by

$$\overline{R}_{e} = \frac{1}{\overline{\sigma}R}$$
, (20)

then

$$\overline{Q} \simeq .48 \left(\overline{R}_{e} c\right)^{-1/2}$$
 (21)

Increasing the conductivity or decreasing the sheet resistance has the opposite effect for the two types of damping. The difference between Equations 15 and 21 arises because Equation 20 is really a second order effect. That is, the E fields parallel to the cavity wall are assumed to be zero in first order. Damping at the walls appears because the E fields at walls are not quite parallel to the walls. Equation 15 is the result of a first order calculation; that is the E field parallel to the damper is non-zero in first order.

#### SECTION 3

#### THEORY

#### 3.1 ONE AND TWO SHEET DAMPERS IN THE FORM OF A CYLINDER WITH OPEN ENDS

In this section we derive the mathematical relationship which relates the position of the damper sheets and their conductivity to the complex frequencies of the cavity. The frequencies are complex because the damper sheets have introduced modal damping. This damping appears in the mathematics as an imaginary part of the new modal frequency. We begin by assuming that we have a cavity in which axisymmetric modes have been established. The cavity, except for the membranes, is empty. The membranes will be assumed to be open ended cylinders; only two membranes will be considered.

Figure 1 depicts the physical situation. The membranes are treated as boundaries between regions I, II and III. In these three, source free regions, Maxwell's equations are

$$\frac{\partial}{\partial \mathbf{r}} \left( \frac{1}{\mathbf{r}} \frac{\partial}{\partial \mathbf{r}} \mathbf{r} \mathbf{B} \right) + \frac{\partial^2 \mathbf{B}}{\partial z^2} - \frac{1}{\mathbf{c}^2} \frac{\partial^2 \mathbf{B}}{\partial \mathbf{t}^2} = 0 , \qquad (22)$$

$$\frac{1}{c} \frac{\partial E_{\mathbf{r}}}{\partial t} = -\frac{\partial B}{\partial z} \quad , \tag{23}$$

and

$$\frac{1}{c} \frac{\partial E_z}{\partial t} = \frac{1}{r} \frac{\partial}{\partial r} (rB) , \qquad (24)$$

where a subscript z or r refers to the z or r cylindrical coordinates respectively, E and B refer to electric and magnetic respectively. Assuming that the time dependence can be represented by  $e^{i\omega t}$  and defining  $k^2 \equiv (\omega/c)^2 - (p\pi/L)^2$  we can solve for the fields in the three regions in terms of a series of Bessel functions and the trigonometric functions  $\sin(p\pi z/L)$  and  $\cos(p\pi z/L)$ ; where p is an integer and L is the height of the cavity. Since this analysis is not really dependent upon the trigonometric functions we suppress them in the equations to follow.

We are really interested in computing the frequencies of oscillation of the system depicted in Figure 1. To do so we must match the solutions in the various regions across the membranes and then finally require  $\mathbf{E}_{_{2}}$  to be equal to zero at the tank wall. In region I the solution is

$$B_{I} = AJ_{I}(kr) , \qquad (25)$$

and from Equations 24 and 25

$$E_{Iz} = -\mathcal{A} \frac{ck}{\omega} iJ_0(kr) . \qquad (26)$$

The symbol  ${\cal A}$  in Equations 4 and 5 represents a constant to be determined; the subscript I represents region I.  $J_q$  are Bessel functions of order q. In region II the fields are

$$B_{II} = eJ_1(kr) + bN_1(kr)$$
, (27)

and

$$E_{\text{II z}} = -i(eJ_0(kr) + bN_0(kr))ck/\omega , \qquad (28)$$

where e and b are constants to be determined and  $\mathbf{N}_q$  is a Neuman function of order  $q_{\,\cdot\,}$  In region III the fields are

$$B_{III} = J_1(kr) + fN_1(kr)$$
, (29)

and

$$E_{III z} = -i(J_0(kr) + fN_0(kr))ck/\omega$$
 (30)

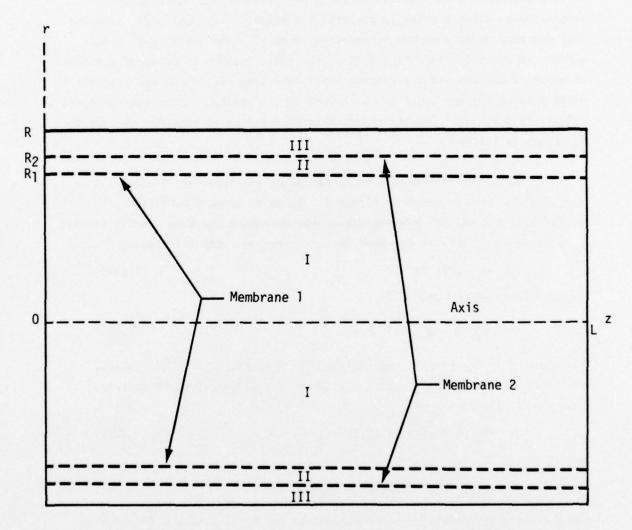


Figure 1. Cross section of a cylinder with membranes.

To find the four constants. 4, b, e, and f we apply the boundary conditions across membranes 1 and 2. The boundary conditions are:

$$B_{II} - B_{I} = 4\pi E_{z}/c R_{e1}$$
,  $r = R_{1}$ , (31)

$$E_{IIz} = E_{1z}$$
, at  $r = R_1$ , (32)

for membrane 1 and

$$B_{III} - B_{II} = 4\pi E_z/c R_{e2}$$
,  $r = R_1$ , (33)

$$E_{IIIz} = E_{IIz}$$
, at  $r = R_2$ , (34)

for membrane 2, where  $\rm R_{eq}$  is the sheet resistance of membrane  $\rm q$  . Inserting Equations 25 through 30 into Equations 31 through 33 we end up with the four equations

$$fa_{11} + ea_{12} + ba_{13} = h_1$$
, (35)

$$fa_{21} + ea_{22} + ba_{23} = h_2$$
, (36)

$$ea_{32} + ba_{33} + aa_{31} = 0$$
, (37)

$$ea_{42} + ba_{43} + aa_{44} = 0$$
, (38)

where

$$a_{11} = -N_{1}(x\alpha_{2}), a_{12} = J_{1}(x\alpha_{2}) - z_{2}J_{0}(x\alpha_{2})$$

$$a_{13} = N_{1}(x\alpha_{2}) - z_{2}n_{0}(x\alpha_{2}), h_{1} = J_{1}(x\alpha_{2})$$

$$a_{21} = -N_{0}(x\alpha_{2}), a_{22} = J_{0}(x\alpha_{2})$$

$$a_{23} = N_{0}(x\alpha_{2}), h_{2} = J_{0}(x\alpha_{2})$$

$$a_{32} = J_{1}(x\alpha_{1}), a_{33} = N_{1}(x\alpha_{1})$$

$$a_{34} = z_{1}J_{0}(x\alpha_{1}) - J_{1}(x\alpha_{1})$$

$$a_{42} = -J_{0}(x\alpha_{1}), a_{43} = -N_{0}(x\alpha_{1})$$

$$a_{44} = J_{0}(x\alpha_{1}), a_{43} = -N_{0}(x\alpha_{1})$$

$$a_{44} = J_{0}(x\alpha_{1}), a_{45} = -N_{0}(x\alpha_{1})$$

and where we have used the definition:

$$kR \equiv x$$
, (40)

$$\alpha_1 \equiv R_1/R$$
 , (41)

$$\alpha_2 \equiv R_2/R , \qquad (42)$$

and

$$z_{1} \equiv i \left(\frac{4\pi}{cR_{e1}}\right) \frac{ck}{\omega}$$

$$z_{2} \equiv i \left(\frac{4\pi}{cR_{e2}}\right) \frac{ck}{\omega} . \tag{44}$$

To find k (or x) we must solve for f in the system of Equations 14 through 17 and set  $E_{\rm III\ z}$  at r = R equal to zero. That is we must solve the region III equation

$$J_0(x) + fn_0(x) = 0 , (45)$$

where we use the relation

$$\frac{ck}{\omega} = \left(1 + \left(\frac{p\pi}{x} \frac{R}{L}\right)^2\right)^{-1/2} , \qquad (46)$$

in  $\mathbf{z}_1$  and  $\mathbf{z}_2$  when we solve for f. If only membrane 2 were present then f would be

$$f = \frac{z_2(j_0(x\alpha_2))^2}{N_0(x\alpha_2)(J_1(x\alpha_2) - z_2J_0(x\alpha_2)) - N_1(x\alpha_2)J_0(x\alpha_2))}.$$
 (47)

Recognizing that

$$J_1(y)N_0(y) - J_0(y)N_1(y) = 2/\pi y$$
, (48)

Equation 47 becomes

$$f = \frac{z_2 (J_0(x\alpha_2))^2}{\frac{2}{\pi x \alpha_2} - z_2 N_0(x\alpha_2) J_0(x\alpha_2)} . \tag{49}$$

Substituting Equation 49 into Equation 45 we find that the equation that must be solved to obtain the complex frequencies, for one membrane, is

$$J_0(x) + \frac{\pi}{2} x \alpha_2 z_2 J_0(x \alpha_2) (N_0(x) J_0(x \alpha_2) - N_0(x \alpha_2) J_0(x)) = 0$$
 (50)

#### 3.2 AN APPROXIMATION FOR ONE AND TWO SHEET DAMPERS

An approximate solution to Equation 50 can be made by assuming that roots  $\mathbf{x}_{\mathrm{np}}$  with the damper ( $\mathbf{z}_{2}$  finite in Equation 50) are not much different than the roots without the damper  $\mathbf{x}_{\mathrm{n}}$ . That is we assume that

$$x_{np} = x_n^0 + \delta_{np} , \qquad (51)$$

where  $\delta_{np}$  is the small change from the zero order root. Under this first order assumption the  $\delta_{np}$  for more than one damper would simply be the sum of the  $\delta_{np}$  for each damper alone. Substituting Equation 51 into Equation 50 and using Equation 46 we find that

$$-J_1 \delta_{np} + i \delta_{np} |z_0| S + i g x_n^0 |z_0| = 0 , \qquad (52)$$

where

$$g(x) \equiv \pi/2\alpha J_0(x\alpha) (N_0(x)J_0(x\alpha) - N_0(x\alpha)J_0(x))$$
, (53)

$$S = g(x_n^0) (1 + A_{np}) + x_n^0 \frac{\partial g}{\partial x_n^0}, \qquad (54)$$

$$A_{np} = L_{np}(1 + L_{np})^{-1}$$
, (55)

$$L_{\rm np} = \left(\frac{p\pi R}{x_{\rm n}^0 L}\right)^2 , \qquad (56)$$

$$|z_0| = \left(\frac{4\pi}{cR_e}\right) \frac{ck_0}{\omega_0} \tag{57}$$

$$\frac{ck_0}{\omega_0} = (1 + L_{np})^{-1/2} , \qquad (58)$$

and where we have used the fact that

$$\frac{\partial J_0}{\partial x} = -J_1 . ag{59}$$

The subscript 2 has also been dropped in Equation 50 since we need only consider one membrane in the present discussion. Letting

$$\delta_{\rm np} = \delta_{\rm np}^{\rm R} + i\delta_{\rm np}^{\rm I} , \qquad (60)$$

in Equation 52 while noting that  $g(x_n^0)$  and S are real numbers we find that

$$\delta_{np}^{I} = \frac{x_{n}^{0} |z_{0}| g(x_{n}^{0}) J_{1}(x_{n}^{0})}{J_{1}^{2}(x_{n}^{0}) + |z_{0}|^{2} s^{2}},$$
(61)

and

$$\delta_{\rm np}^{\rm R} = -\frac{|z_0|^2 x_{\rm n}^0 g(x_{\rm n}^0)}{J_1^2 (x_{\rm n}^0) + |z_0|^2 s^2} \ . \tag{62}$$

From Equation 53 with the knowledge that  $\mathbf{x}_n^0$  is a root of  $\mathbf{J}_0$  it can easily be shown that

$$g(x_n^0) = \beta J_0^2(x_n^0 \alpha) N_0(x_n^0) , \qquad (63)$$

and that

$$S = \beta J_0(x_n^0 \alpha) \left[ N_0(x_n^0) J_0(x_n^0 \alpha) (1 + A_{np}) + x_n^0 (-2\alpha N_0(x_n^0) J_1(x_n^0 \alpha) + N_0(\alpha x_n^0) J_1(x_n^0) - N_1(x_n^0) J_0(x_n^0 \alpha) \right],$$

$$(64)$$

where

$$\beta \equiv \frac{\pi}{2} \alpha . \tag{65}$$

Note that  $N_0(x_n^0)$  is almost equal to  $J_1(x_n^0)$  in Equation 61 so that  $\delta_{np}^I$  is positive definite.

Equations 61 and 62 are the equations which show how the wave number of the cavity mode changes when a damper shell is introduced into a cylindrical cavity. In order to investigate the modal damping we will first need to express the new modal frequency in terms of  $\delta^{\rm I}_{\rm np}$ . We will then optimize the damping for a particular mode by finding what value of  $^{\rm R}_{\rm e}$  makes the imaginary portion of the angular frequency,  $\omega^{\rm I}_{\rm np}$ , a maximum for a given damper position. The frequency  $\omega_{\rm np}$ , for the n,p mode of a tank is

$$\left(\frac{\omega_{\rm np}}{c}\right)^2 = \frac{x_{\rm n}^2}{R^2} + \left(\frac{p\pi}{L}\right)^2 , \tag{66}$$

where we have used Equations 40 and 46. Substituting Equation 51 into 66 we find that

$$\omega_{\rm np}^{\rm I} = \frac{c}{R} \delta_{\rm np}^{\rm I} \left( 1 + \left( \frac{p\pi R}{x_{\rm n}^0 L} \right)^2 \right)^{-1/2} . \tag{67}$$

We therefore see that maximizing the damping of the n,p mode requires maximizing  $\delta_{np}^{I}$ . Taking the derivative of  $\delta_{np}^{I}$  with respect to  $|z_{0}|$  in Equation 61 and setting the result equal to zero we find the value of  $|z_{0}|$ ,  $|z_{0}|_{M}$  which makes  $\delta_{np}^{I}$  a maximum:

$$|z_0|_{M} = \sqrt{J_1^2/S^2} \ . \tag{68}$$

Substituting Equation 70 into 69 we find the value of  $\delta_{np}^{I}$ ,  $(\delta_{np}^{I})_{M}$ , which is maximum for a given position of the damper, namely

$$(\delta_{np}^{I})_{M} = .5|g(x_{n}^{0})/S|x_{n}^{0}$$
 (69)

Note that  $(\delta_n^I)$  will be zero (when E<sub>z</sub> is zero) if the damper position is at the wall of the cylinder. That is when  $J_0(\alpha x_n^0) = 0$ . This result is in direct contrast to Equation 10 which implies that damping should be best at

the wall. As noted in Section 2, Equation 10 was derived under an erroneous assumption for the functional dependence of the field. Equation 69 is one of the equations we will be discussing in the next section. It, together with Equation 67, describe how the damping constant for the np mode depends upon position of the damper. Equation 68 contains the information necessary to determine the resistance of the damper sheet necessary for optimum damping. Using Equations 63, 68 and 61 we can put Equation 70 into a directly usable form

$$R_{e} = 120\pi \left(1 + \left(\frac{p\pi R}{x_{n}^{0}L}\right)^{2}\right)^{-1/2} |J_{1}/S| \quad (ohms) \quad . \tag{70}$$

Equation 70 will also be discussed in the next section.

## SECTION 4 RESULTS

In this section we will evaluate the optimum damping resistance from Equation 70 for a number of n,p modes as a function of damper position. We will also evaluate  $\delta_{np}$  with the optimum resistance as a function of damper position, for a number of modes. The restriction on  $\delta_{np}$  will be that it must be smaller than  $x^0_{np}$  for the damping constant to be meaningful. How the damping changes as the resistance deviates from the optimum value is also discussed. Finally a table of values of Q for modes,  $5 \le n \le 1$   $0 \le p \le 10$ , is constructed for a sheet damper at two positions,  $\alpha = .8$  and  $\alpha = .92$ . These two positions correspond, roughly, to the sheet damper positions in the Physics International (PI) tank during the MRC March 1977 photon experiments.

Figures 2 through 4 are plots, for three representative values of p, of optimum resistance vs. damper position divided by the cylinder radius  $(\alpha)$ . The labels A to E correspond to n = 1 to 5 respectively. In general the resistances oscillate (except for n = 1) between zero and some larger value. Larger values of resistance occur for larger n's but, in general, decrease for increasing p. (n is associated with the number of nodes in the r direction and p with the number of nodes in the z direction.) The reduction of resistance with increasing p is associated with the fact that as p increases the electric field in the z direction becomes a smaller fraction of the total electric field so that a larger sheet current is necessary (smaller resistance) to obtain optimum damping. Figures 5 through 19 are a selection of  $\delta_{\rm np}^{\rm I}$  vs.  $\alpha$ . In conjunction with Equation 67 they can be used for designing a damper for modes

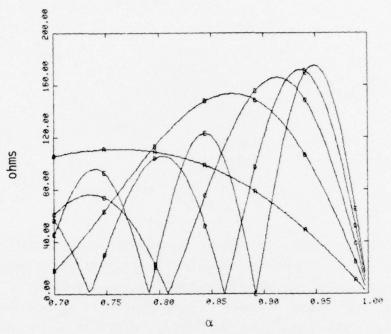


Figure 2. Optimum resistance vs.  $\alpha$ , for p = 0, n  $\leq$  5.

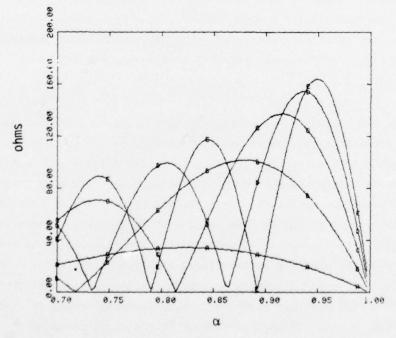


Figure 3. Optimum resistance vs.  $\alpha$ , p = 5, n  $\leq$  5.

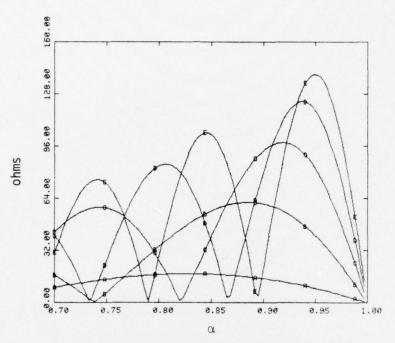


Figure 4. Optimum resistance vs.  $\alpha$ , p = 10, n = 5.

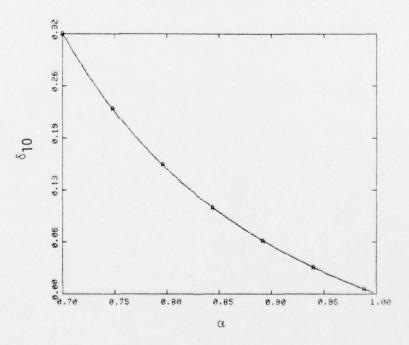


Figure 5.  $\delta_{10}^{I}$  vs.  $\alpha$ .

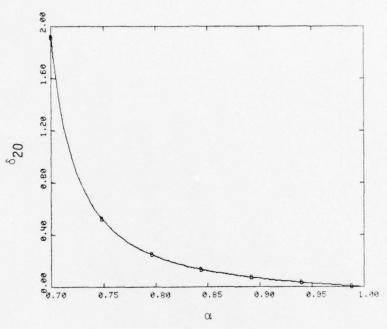


Figure 6.  $\delta_{20}^{I}$  vs.  $\alpha$ .

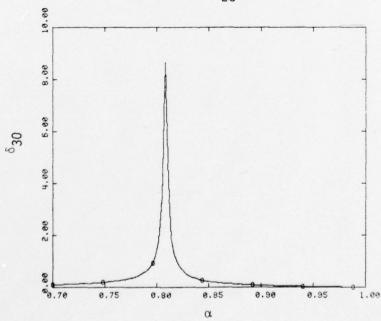


Figure 7.  $\delta_{30}^{I}$  vs.  $\alpha$ .

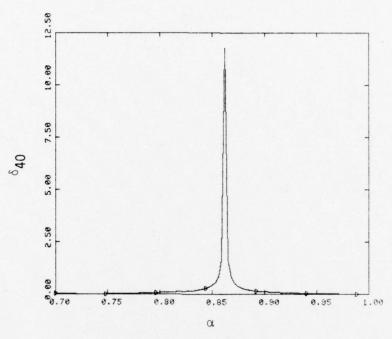


Figure 8.  $\delta_{40}^{I}$  vs.  $\alpha$ .

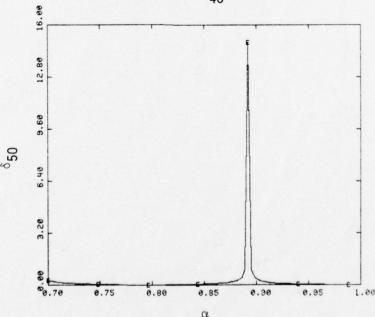


Figure 9.  $\delta_{50}^{I}$  vs.  $\alpha$ .

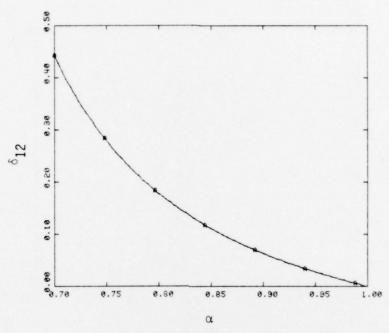


Figure 10.  $\delta_{12}^{I}$  vs.  $\alpha$ .

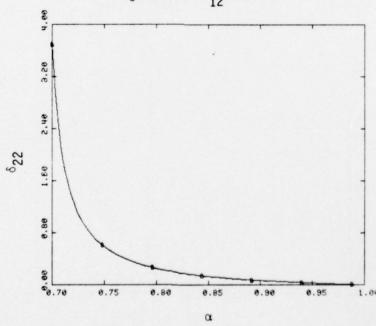
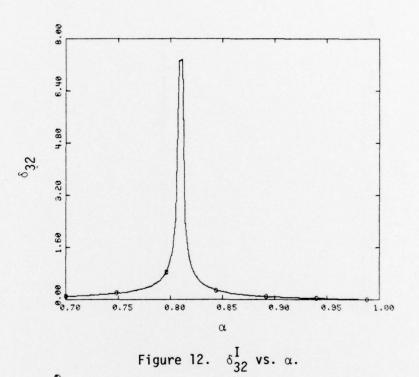


Figure 11.  $\delta_{22}^{I}$  vs.  $\alpha$ .



7.50

10.00

Figure 13.  $\delta_{\mbox{42}}^{\mbox{I}}$  vs.  $\alpha.$ 

0.80

0.75

0.85

α

1.00

0.95

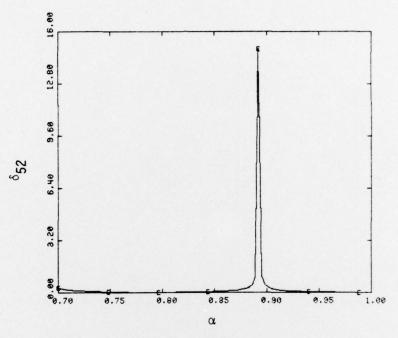


Figure 14.  $\delta_{52}^{I}$  vs.  $\alpha$ .

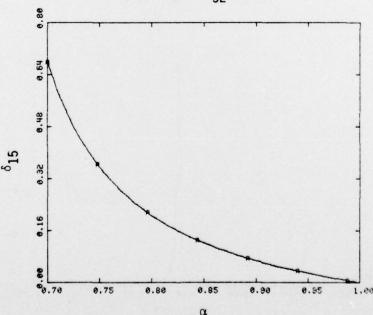
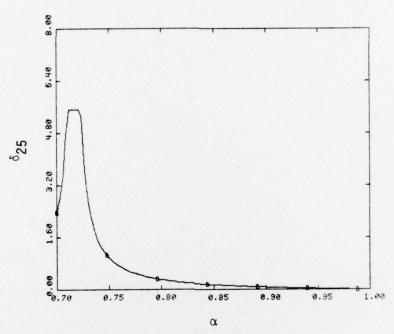


Figure 15.  $\delta_{15}^{I}$  vs.  $\alpha$ .



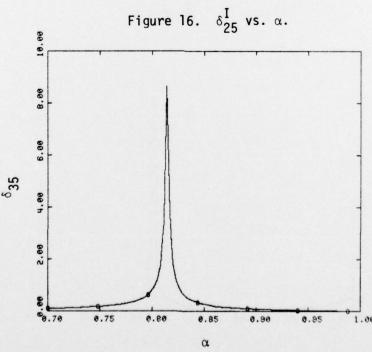


Figure 17.  $\delta_{35}^{I}$  vs.  $\alpha$ .

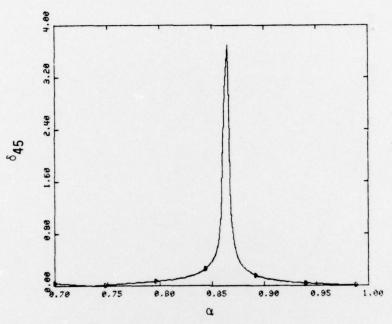


Figure 18.  $\delta_{\mbox{45}}^{\mbox{I}}$  vs.  $\alpha.$ 

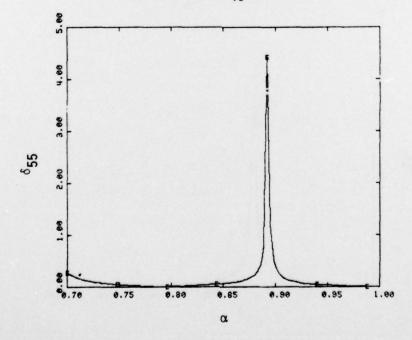


Figure 19.  $\delta_{55}^{I}$  vs.  $\alpha$ .

of a cylindrical cavity. The restriction on their use is that the figures are to be considered valid when  $\delta_{np} < x_n^0$  ,

$$x_n^0 = 2.405, 5.520, 8.654,$$
  
 $x_n^0 \simeq n\pi - \pi/4.$ 

In Figures 5 through 19 the curves are plotted for a useful  $\alpha$  range  $.7 \le \alpha \le 1$ . The curves are truncated for  $\delta_{np} \sim x_n^0$  (for example  $\delta_{25}$  in Figure 16 appears flat at the peak where  $\delta_{25} \ge x_2^0$ ).

We now use Figures 2 through 19, and similar curves which are not presented, to construct a table of Q's for modes  $1 \le n \le 5$   $0 \le p \le 10$  for a two sheet damper. To construct this table we first develop an expression for the Q for the n,p mode of a cylindrical cavity,  $Q_{np}$ . Beginning from Equation 67 the time,  $t_{np}$ , for the fields to decay to  $e^{-1}$  of their initial value is

$$t_{\rm np} = \frac{R}{c\delta_{\rm np}^{\rm I}} (1 + L_{\rm np})^{1/2} ,$$
 (71)

where  $L_{np}$  is given by Equation 56. Since the energy goes as the fields squared the time  $T_{np}$  (defined as the damping time) for the energy to decay to  $e^{-1}$  of its initial value is

$$T_{np} = .5 t_{np} . (72)$$

Thus from Equations 72 and 71, the expression for the period of the n,p mode

$$\tau_{\rm np} = \frac{2\pi R}{{\rm cx}_{\rm n}^0} \left(1 + L_{\rm np}\right)^{-1/2} , \qquad (73)$$

and the definition

$$Q_{np} = \frac{T_{np}}{\tau_{np}} , \qquad (74)$$

we have

$$Q_{\rm np} = \frac{1}{4\pi} \frac{x_{\rm n}^0}{\delta_{\rm np}^{\rm I}} (1 + L_{\rm np}) . \tag{75}$$

It is interesting to note that  $\mathbf{Q}_{n0}$  is independent of the dimensions of the tank;  $\mathbf{Q}_{n0}$  is dependent on the relative positions of the dampers, however.

We construct Table 1 by looking up values of  $\delta_{np}$  in the figures adding them for the two damper sheets, at  $\alpha$  = .8 and .92, and inserting the values in Equation 75 where we take R/L = 1/3, roughly the dimensions of the PI vacuum tank. For example  $Q_0$  is constructed in the following way: from Figure 5  $\delta_{10}^{I}$  for  $\alpha$  = .8 is .155 and  $\delta_{10}^{I}$  for  $\alpha$  = .92 is .047. Adding the total  $\delta_{10}^{I}$  is .20. Since  $L_{10}$  is zero

$$Q_{10} = \frac{1}{4\pi} \frac{(2.4)}{.2} = .95$$
.

Tables 4 and 5 are constructed by looking up the values for  $R_e$  on Figures 2 through 4 and similar figures not presented in this report. Tables indicates how valid the approximation  $x_n^0/\delta_{np}^I>1$  is. Table 3 indicates what the actual damping times are for the n,p modes of the PI tank (R  $\cong$  2 m, L  $\cong$  6 m) with optimum resistance dampers placed at  $\alpha$  = .8 and  $\alpha$  = .92.

We now consider the effect on  $\delta_{np}^{I}$  for deviations away from the optimum resistance value. Our goal is to determine the effect on  $Q_{np}$  for a damper that is not optimized with respect to resistance. If  $U_{np}$  represents the ratio of the non-optimized  $\delta_{np}^{I}$  to  $(\delta_{np}^{I})_{M}$  (Equation 69) and  $z_{np}$  represents the ratio of the non-optimized  $|z_{0}|$  (see Equation 57) to  $|z_{0}|_{M}$  (Equation 68) then by means of Equations 61, 68 and 69 we can show that

$$U_{\rm np} = \frac{2 z_{\rm np}}{1 + (z_{\rm np})^2} \,. \tag{76}$$

Figure 20 is a plot of Equation 76 and can be used to find  $Q_{np}$  for a damper of arbitrary resistance. For example if the actual resistance of the damper

Table 1. Q(n,p) for two damper sheets at  $\alpha$  = .8 and  $\alpha$  = .92.

n	0	1	2	3	4	5	6	7	8	9	10
1	.956	1.09	1.49	2.15	3.08	4.28	5.74	7.47	9.46	11.7	14.2
2	1.54	1.57	1.67	1.83	2.06	2.35	2.70	3.11	3.59	4.13	4.73
3	.485	.511	.588	.715	.891	1.11	1.38	1.70	2.06	2.47	2.93
4	6.68	6.73	6.89	7.16	7.53	8.02	8.60	9.30	10.1	11.0	12.0
5	11.8	11.8	12.0	12.2	12.5	13.0	13.5	14.1	14.9	15.7	16.6

Table 2.  $X_n/\delta_{np}^I$  for two damper sheets at  $\alpha$  = .8 and  $\alpha$  = .92.

2	0	1	2	3	4	5	6	7	8	9	10
1	12.0	11.5	10.6	10.0	9.62	9.38	9.22	9.12	9.05	9.00	8.96
2	19.4	19.1	18.4	17.4	16.4	15.5	14.8	14.1	13.6	13.2	12.9
3	61.0	6.33	6.98	7.93	9.07	10.2	11.4	12.4	13.4	14.2	14.9
4	83.9	83.9	84.0	84.0	84.1	84.1	84.2	84.3	84.3	84.3	84.3
5	148	148	148	147	145	145	144	143	142	141	140

Table 3. Damping time  $\mathsf{T}_{np}$  for TM cylindrical tank modes (in nanoseconds).

1/2	0	1	2	3	4	5	6	7	8	9	10
1	33.3	34.8	39.2	45.7	53.6	62.3	71.6	81.2	91.0	101	111
2	23.4	23.5	23.7	24.2	24.9	25.9	27.1	28.4	30.0	31.7	33.5
3	4.70	4.91	5.53	6.51	7.76	9.24	10.8	12.5	14.3	16.2	18.1
4	47.5	47.6	48.2	49.2	50.5	52.1	54.0	56.1	58.5	61.1	63.8
5	66.3	66.4	66.7	67.3	68.0	69.0	70.1	71.5	73.0	74.7	76.5

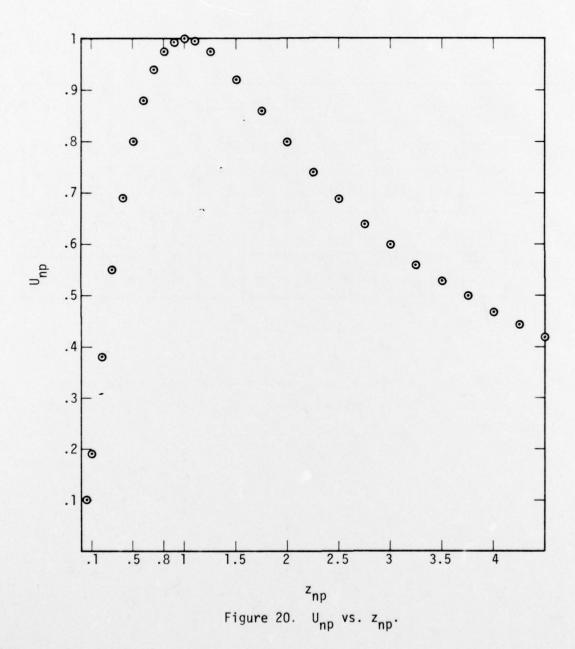
Table 4. Optimum resistance (ohms) for sheet at  $\alpha$  = .8.

n	0	1	2	3	4	5	6	7	8	9	10
1	109	94.6	70.9	53.1	41.5	33.7	28.4	24.4	21.4	19.1	17.1
2	116	113	102	89.9	77.1	65.1	56.6	56.6	42.6	38.4	33.9
3	17.4	16.1	19.2	19.3	21.3	24.6	24.5	24.5	27.2	26.1	27.1
4	105	105	104	103	101	98.4	96.1	93.3	90.0	87.2	83.7
5	30.6	33.8	30.3	33.2	32.7	28.9	31.3	30.5	26.8	28.8	25.2

Table 5. Optimum resistance (ohms) for sheet at  $\alpha$  = .92.

n	0	1	2	3	4	5	6	7	8	9	10
1	62.9	56.2	45.5	35.6	28.8	24.2	20.5	17.8	15.8	14.1	17.1
2	130	127	120	110	99.4	90.1	80.7	73.0	66.7	60.6	33.9
3	165	163	159	153	145	137	128	120	66.7	105	27.1
4	160	160	156	154	149	143	138	132	112	119	83.7
5	115	119	114	116	113	107	107	103	124	95.4	25.2

is twice the optimum value then  $\delta_{np}^I$  will be 80 percent of the optimum value. Since  $Q_{np}$  varies inversely as  $\delta_{np}^I$ ,  $Q_{np}$  will be 25 percent larger than optimum.



### SECTION 5 CONCLUSIONS

In Section 2 of this report we discussed the basic physical concepts underlying resistive sheet dampers by means of an oversimplified example. In Sections 3 and 4 we obtained the actual equations for two cylindrical dampers with no end caps. The equations were solved in first order. Table 1 indicates that many of the modes damp to e<sup>-1</sup> of their initial value in about one modal period. Tables 4 and 5 indicate that, depending on the particular mode to be damped, the optimum sheet resistance can vary from 14 to 165 ohms. Although damping isn't a rapidly varying function of resistance it is still important, in building the damper, to have some idea what modes need to be damped.

The cylindrical sheet damper, with no end caps, becomes an increasingly poorer damper, as the frequency of the cavity increases (if the increasing frequency is due to an increasing number of nodes in the z direction only). As the frequency increases in this manner a smaller percentage of the electric field energy is associated with the z direction. Since it is the electric field in the z direction that causes the absorption of energy by the damper the cylindrical sheet damper with no end caps becomes a poorer damper. If one were interested in damping these higher frequency TM modes it would be necessary to add end caps to the damper.

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